

# Financing Constraints, Firm Dynamics and Innovation

Andrea Caggese  
(UPF and Barcelona GSE)

May 17, 2013

# Motivation (1)

- The process of firm entry, growth and exit is largely driven by technological progress.
  - New entrants adopt technologies at the frontier and are more productive than existing units.
  - Firms that successfully innovate grow, while unsuccessful ones shrink and disappear.
- These dynamics determine aggregate productivity growth.
- Do financial factors matter? If yes, how? directly (lack of finance to invest in innovation) or indirectly (affecting entry-exit and competition)?

# Motivation (2)

A recent paper by Hsieh and Klenow (2012) compares life cycle profile of manufacturing plants in USA, Mexico and India:

Figure 4: Employment Growth over the Life-Cycle

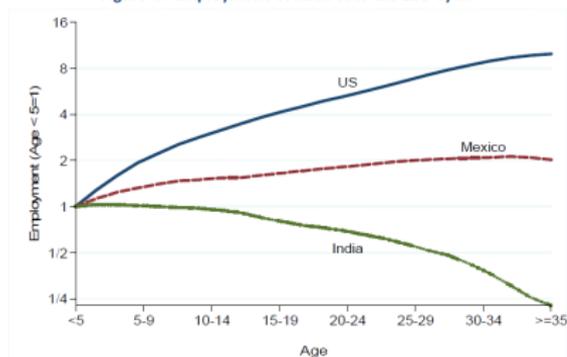
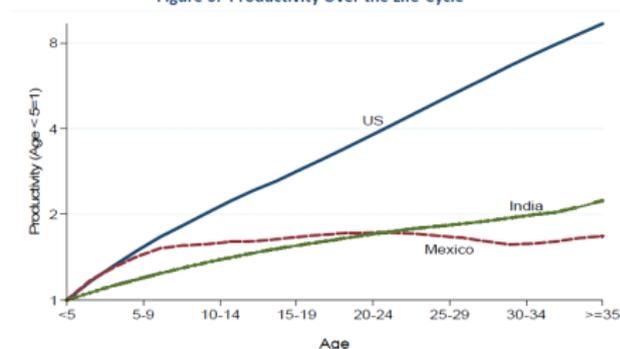


Figure 6: Productivity Over the Life-Cycle



# This paper - preview of empirical results

- Empirical evidence from firm level Italian data (with balance sheet data, innovation data, and survey information on financing frictions).

# This paper - preview of empirical results

- Empirical evidence from firm level Italian data (with balance sheet data, innovation data, and survey information on financing frictions).
- I find that in sectors with more financing frictions:

# This paper - preview of empirical results

- Empirical evidence from firm level Italian data (with balance sheet data, innovation data, and survey information on financing frictions).
- I find that in sectors with more financing frictions:
  - Productivity grows slower over the firm life cycle.

# This paper - preview of empirical results

- Empirical evidence from firm level Italian data (with balance sheet data, innovation data, and survey information on financing frictions).
- I find that in sectors with more financing frictions:
  - Productivity grows slower over the firm life cycle.
  - Firms do less R&D to introduce new products and more R&D to improve current products or productive processes

# This paper - preview of empirical results

- Empirical evidence from firm level Italian data (with balance sheet data, innovation data, and survey information on financing frictions).
- I find that in sectors with more financing frictions:
  - Productivity grows slower over the firm life cycle.
  - Firms do less R&D to introduce new products and more R&D to improve current products or productive processes
- ...than in sectors with less financing frictions.

# This paper - preview of empirical results

- Empirical evidence from firm level Italian data (with balance sheet data, innovation data, and survey information on financing frictions).
- I find that in sectors with more financing frictions:
  - Productivity grows slower over the firm life cycle.
  - Firms do less R&D to introduce new products and more R&D to improve current products or productive processes
- ...than in sectors with less financing frictions.
- Correlation, not a proof of causation. So I need a model.

# This paper - Model Introduction

- Industry model with heterogenous firms, entry and exit, costly bankruptcy and two different types of innovation:
  - ① Type-one, More risky: If it fails, profits drop relative to pre-innovation level.

# This paper - Model Introduction

- Industry model with heterogenous firms, entry and exit, costly bankruptcy and two different types of innovation:
  - ① Type-one, More risky: If it fails, profits drop relative to pre-innovation level.
    - Intuition: embodied innovation: requires new equipment that embodies the new technology and cannot be adapted back to produce the previous products (similar to the concept of "radical innovation" in management science).

# This paper - Model Introduction

- Industry model with heterogenous firms, entry and exit, costly bankruptcy and two different types of innovation:
  - ① Type-one, More risky: If it fails, profits drop relative to pre-innovation level.
    - Intuition: embodied innovation: requires new equipment that embodies the new technology and cannot be adapted back to produce the previous products (similar to the concept of "radical innovation" in management science).
  - ② Type-two, Less risky: if it fails, profits are at the minimum equal to pre-innovation level.

# This paper - Model Introduction

- Industry model with heterogenous firms, entry and exit, costly bankruptcy and two different types of innovation:
  - 1 Type-one, More risky: If it fails, profits drop relative to pre-innovation level.
    - Intuition: embodied innovation: requires new equipment that embodies the new technology and cannot be adapted back to produce the previous products (similar to the concept of "radical innovation" in management science).
  - 2 Type-two, Less risky: if it fails, profits are at the minimum equal to pre-innovation level.
    - Intuition: disembodied innovation: new ideas/improvements which may increase productivity, but which never reduce previous levels.

# This paper - Model Introduction

- Industry model with heterogenous firms, entry and exit, costly bankruptcy and two different types of innovation:
  - ① Type-one, More risky: If it fails, profits drop relative to pre-innovation level.
    - Intuition: embodied innovation: requires new equipment that embodies the new technology and cannot be adapted back to produce the previous products (similar to the concept of "radical innovation" in management science).
  - ② Type-two, Less risky: if it fails, profits are at the minimum equal to pre-innovation level.
    - Intuition: disembodied innovation: new ideas/improvements which may increase productivity, but which never reduce previous levels.
- Link with empirical data: in a previous paper, I show that in my dataset R&D to introduce new products is more risky (it generates more volatility in profits) than the other types of R&D.

# This paper - Preview of Model results

- I compute the industry equilibrium for different technology types and different intensity of financing frictions.

# This paper - Preview of Model results

- I compute the industry equilibrium for different technology types and different intensity of financing frictions.
- With type-one (more risky) innovation, financing frictions reduce the frequency of innovation and aggregate productivity. Opposite result with "type-two" innovation.

# This paper - Preview of Model results

- I compute the industry equilibrium for different technology types and different intensity of financing frictions.
- With type-one (more risky) innovation, financing frictions reduce the frequency of innovation and aggregate productivity. Opposite result with "type-two" innovation.
- Intuition for the result: financing frictions reduce entry and competition.

# This paper - Preview of Model results

- I compute the industry equilibrium for different technology types and different intensity of financing frictions.
- With type-one (more risky) innovation, financing frictions reduce the frequency of innovation and aggregate productivity. Opposite result with "type-two" innovation.
- Intuition for the result: financing frictions reduce entry and competition.
  - They increase the upside gain (increase in profits if innovation is successful)

# This paper - Preview of Model results

- I compute the industry equilibrium for different technology types and different intensity of financing frictions.
- With type-one (more risky) innovation, financing frictions reduce the frequency of innovation and aggregate productivity. Opposite result with "type-two" innovation.
- Intuition for the result: financing frictions reduce entry and competition.
  - They increase the upside gain (increase in profits if innovation is successful)
  - ... but also the downside risk (firms that do not innovate remain profitable for longer time)

# This paper - Preview of Model results

- I compute the industry equilibrium for different technology types and different intensity of financing frictions.
- With type-one (more risky) innovation, financing frictions reduce the frequency of innovation and aggregate productivity. Opposite result with "type-two" innovation.
- Intuition for the result: financing frictions reduce entry and competition.
  - They increase the upside gain (increase in profits if innovation is successful)
  - ... but also the downside risk (firms that do not innovate remain profitable for longer time)
  - When innovation has a downside risk, the more financing frictions (or other barriers that raise entry costs), the less innovation and aggregate productivity in the industry.

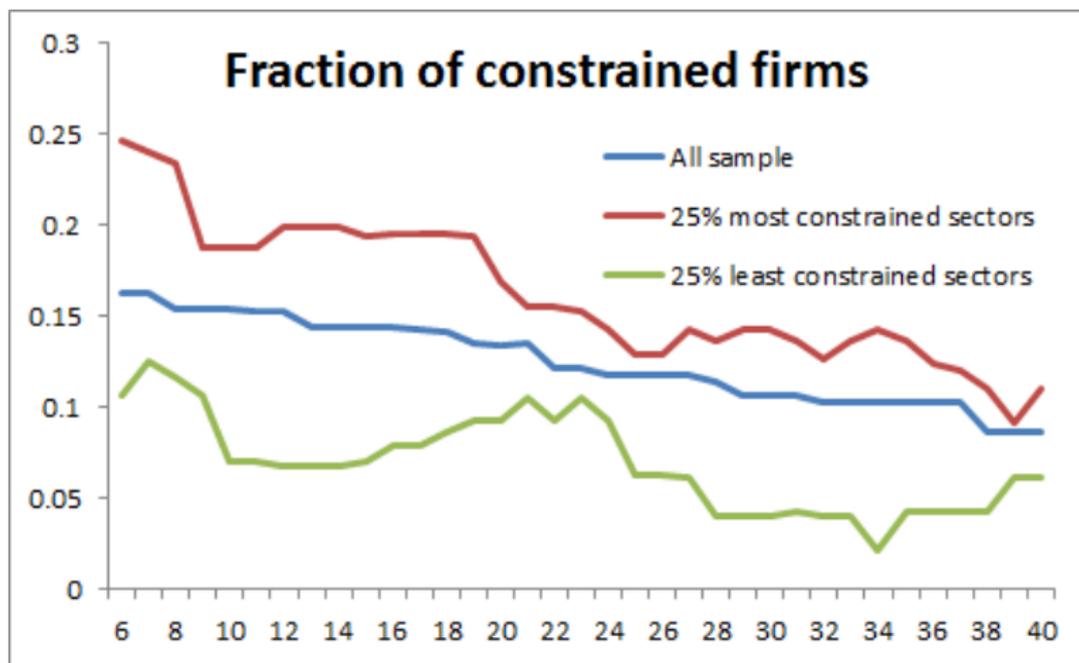
# Empirical data

- Construct a survey measure of financing constraints.
- Calculate the percentage of financially constrained firms in each 4 digit manufacturing industry
- Create two groups:
  - The 25% four digit sectors with most constrained firms, called the "Constrained" group,
  - The 25% four digit sectors with least constrained firms, called the "Unconstrained" group.
- Calculate age profile of innovation and productivity.

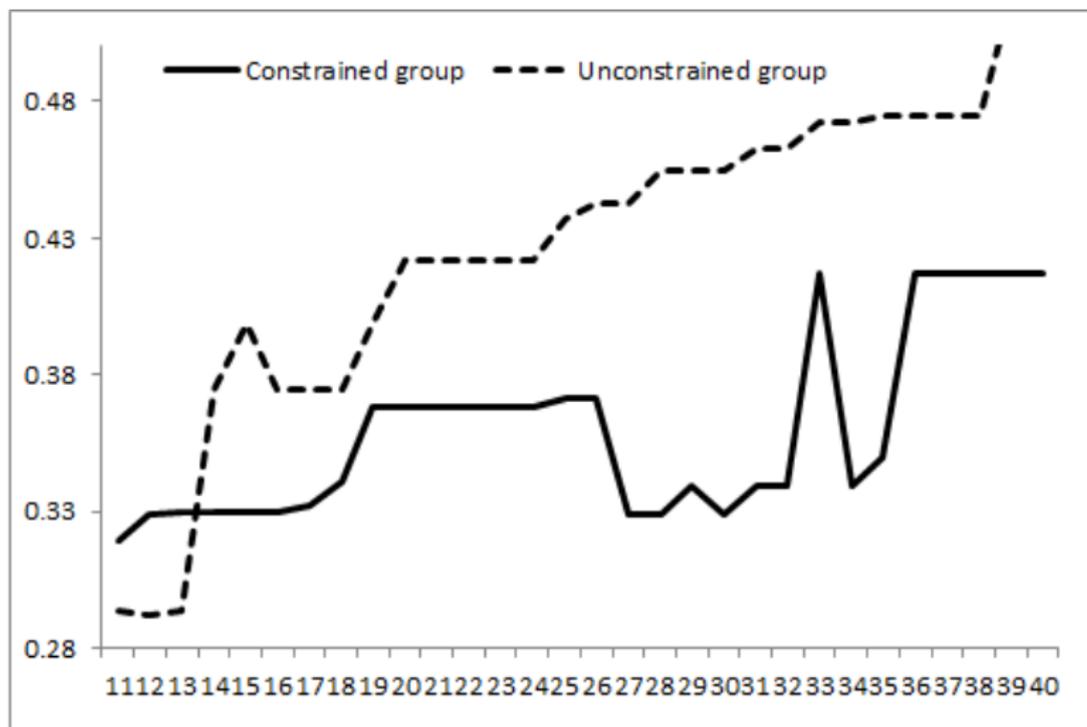
## group composition

2 digit sector	n. obs.	% of firms in "Constrained" group	% of firms in "Unconstr." group
Food and Drinks	960	74%	13%
Textiles	1150	26%	25%
Shoes and Clothes	551	38%	62%
Wood Furniture	343	36%	21%
Paper	379	37%	28%
Printing	457	51%	37%
Chemical, Fibers	614	43%	34%
Rubber and Plastic	717	21%	0%
Non metallic products	823	37%	7%
Metals	614	35%	19%
Metallic products	1183	61%	15%
Mechanical Products	2031	22%	30%
Electrical Products	522	21%	10%
Television and comm.	303	4%	0%

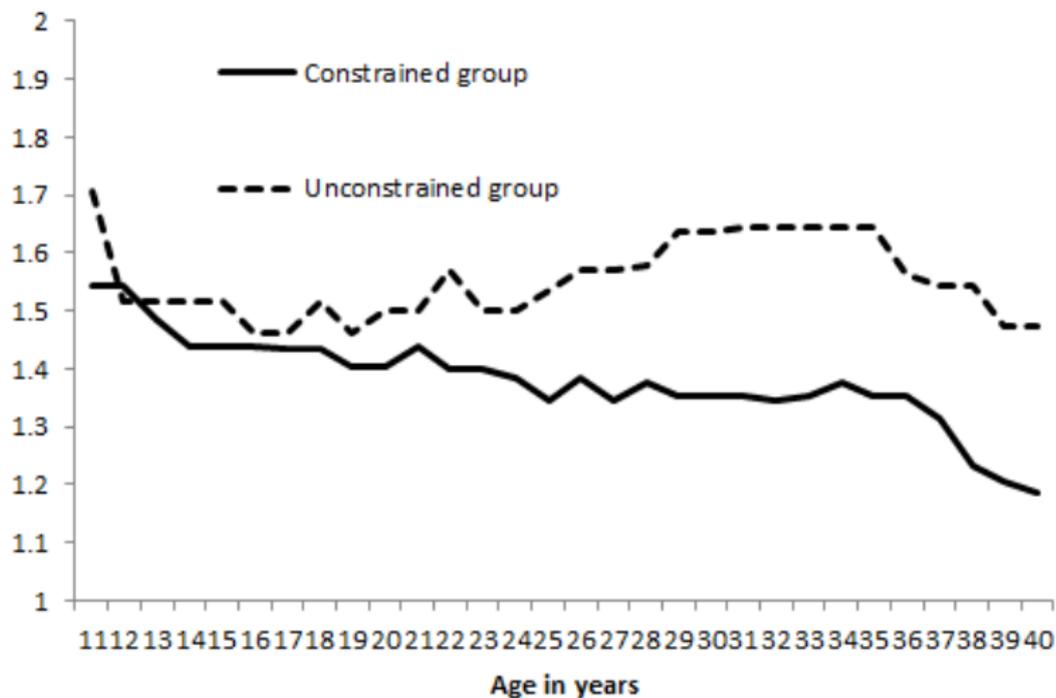
## Fraction of constrained firms over age



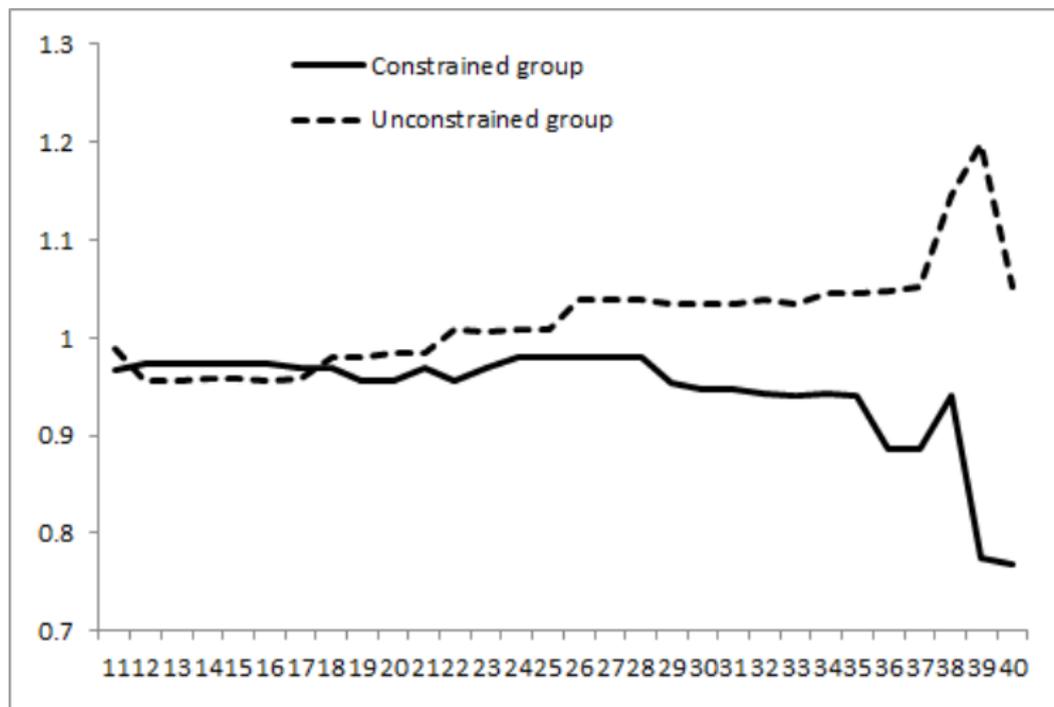
## Percentage of innovating firms (doing R&amp;D)



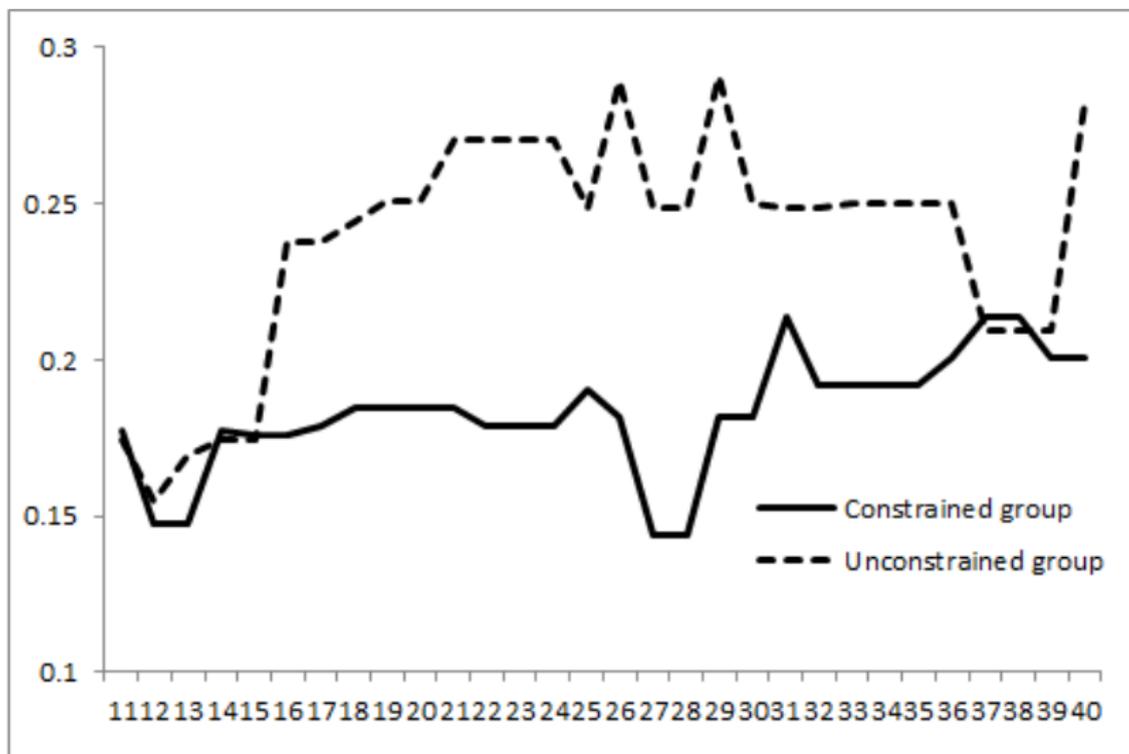
# Total factor productivity conditional on age



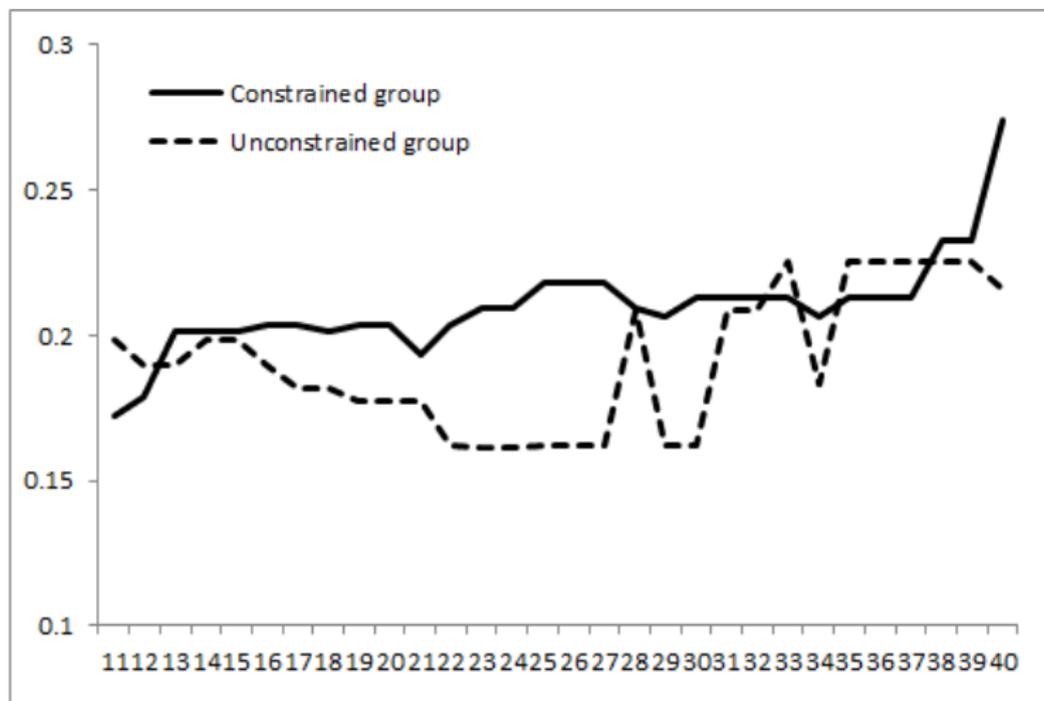
# Total Factor productivity conditional on age, relative to TFP conditional on age in the 2 digit sector.



# Percentage of firms doing R&D to introduce new products over age.



# Percentage of firms doing R&D to improve current products or productive processes.



# The model

- Each firm in an industry uses labour (wage=1) to produce a variety  $w \in \Omega$  of a consumption good.
- Consumers preferences for the varieties in the industry are C.E.S. with elasticity  $\sigma > 1$ .
- One-off fixed cost to enter  $S^C$
- Per-period fixed costs of production  $F$

# Demand

The C.E.S. price index  $P_t$  is then equal to:

$$P_t = \left[ \int_w p_t(w)^{1-\sigma} \right]^{\frac{1}{1-\sigma}}$$

The associated quantity of the aggregated differentiated good  $Q_t$  is:

$$Q_t = \left[ \int_w q_t(w)^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

The overall demand for the differentiated good  $Q_t$  is generated by:

$$Q_t = AP_t^{1-\eta}$$

# Profit function

Profits for a generic firm with productivity  $v_t$  :

$$\pi_t(v_t, \varepsilon_t) = \frac{(\sigma - 1)^{\sigma-1}}{\sigma^\sigma} AP_t^{\sigma-\eta} v_t^{\sigma-1} - F_t$$

$$F_t = F + \varepsilon_t$$

$\varepsilon_t$  follows an I.I.D. process. It implies that sometimes profits  $\pi_t(v_t, \varepsilon_t)$  are negative.

The marginal cost of production is equal to  $1/v_t$ .

# Innovation - 1

- Marginal productivity at the frontier grows at the gross rate  $g > 1$ . Labour cost grows at the same rate (simplifying assumption) → marginal production cost  $1/\nu_t$  for a firm depends on its technology level relative to frontier.
- New firms start with technologies close to the frontier.
  - If they do not innovate: with probability  $\zeta^{NI}$  they keep up with the frontier (relative productivity  $\nu_t$  remains constant), otherwise  $\nu_t$  depreciates at the rate  $g$  (obsolescence).

# Innovation - 1

- Marginal productivity at the frontier grows at the gross rate  $g > 1$ . Labour cost grows at the same rate (simplifying assumption) → marginal production cost  $1/\nu_t$  for a firm depends on its technology level relative to frontier.
- New firms start with technologies close to the frontier.
  - If they do not innovate: with probability  $\zeta^{NI}$  they keep up with the frontier (relative productivity  $\nu_t$  remains constant), otherwise  $\nu_t$  depreciates at the rate  $g$  (obsolescence).
  - If they innovate, with probability  $\zeta^I$  they get to the frontier, otherwise  $\nu_t$  depreciates at the rate  $g^{fail}$

# Innovation - 2

- Type 1 Embodied (risky) innovation:  $g^{fail} > g$  :

$$\begin{array}{ccc}
 \text{Innovation} & \text{Does not} & \text{Innovation} \\
 \text{succeeds} & \text{innovate and} & \text{fails} \\
 & \text{depreciates} & \\
 \underbrace{(v_{t+1} = 1)} & > \underbrace{\left(v_{t+1} = \frac{v_t}{g}\right)} & > \underbrace{\left(v_{t+1} = \frac{v_t}{g^{fail}}\right)}
 \end{array}$$

- Type 1 Disembodied innovation:  $g^{fail} \leq g$  :

$$\begin{array}{ccc}
 \text{Innovation} & \text{Innovation} & \text{Does not} \\
 \text{succeeds} & \text{fails} & \text{innovate and} \\
 & & \text{depreciates} \\
 \underbrace{(v_{t+1} = 1)} & > \underbrace{\left(v_{t+1} = \frac{v_t}{g^{fail}}\right)} & \geq \underbrace{\left(v_{t+1} = \frac{v_t}{g}\right)}
 \end{array}$$

# Timing and Financing frictions

- Budget constraint:

$$a_t = R(a_{t-1} - I_{t-1}K) + \pi_t(v_t, \varepsilon_t) \quad (1)$$

- $I_{t-1}$  is an indicator function that is equal to 1 if the firm decided to innovate in period  $t - 1$ .
- Firms need to pay in advance the fixed costs of production  $F$  and of innovation  $K$  :
- Continuation is feasible only if:

$$a_t \geq F \quad (2)$$

- Innovation is feasible only if:

$$a_t \geq F + K \quad (3)$$

# Value functions

Value function today conditional innovating:

$$V_t^{UP} (a_t, \varepsilon_t, v_t) = -K + \frac{1 - \delta}{R} \left\{ \begin{aligned} & \zeta^I E_t [V_{t+1} (a_{t+1}, \varepsilon_{t+1}, 1) + \pi_{t+1} (\varepsilon_{t+1}, 1)] + (1 - \zeta^I) \\ & E_t \left[ V_{t+1} \left( a_{t+1}, \varepsilon_{t+1}, \frac{v_t}{g^{fail}} \right) + \pi_{t+1} \left( \varepsilon_{t+1}, \frac{v_t}{g^{fail}} \right) \right] \end{aligned} \right\}$$

Likewise, the value function conditional on not innovating is:

$$V_t^{NOUP} (a_t, \varepsilon_t, v_t) = \frac{1 - \delta}{R} \left\{ \begin{aligned} & \zeta^{NI} E_t [V_{t+1} (a_{t+1}, \varepsilon_{t+1}, v_t) + \pi_{t+1} (\varepsilon_{t+1}, v_t)] \\ & + (1 - \zeta^{NI}) E_t \left[ V_{t+1} \left( a_{t+1}, \varepsilon_{t+1}, \frac{v_t}{g} \right) + \pi_{t+1} \left( \varepsilon_{t+1}, \frac{v_t}{g} \right) \right] \end{aligned} \right\}$$

# Policy functions

The firm innovates and chooses  $I_t(a_t, \varepsilon_t, v_t) = 1$  if both the following conditions are satisfied:

$$V_t^{UP}(a_t, \varepsilon_t, v_t) > V_t^{NOUP}(a_t, \varepsilon_t, v_t)$$

$$a_t \geq F + K$$

Given the innovation decision, the value of the firm at time  $t$  is:

$$V_t(a_t, \varepsilon_t, v_t) = \tag{4}$$

$$1(a_t \geq F) \left\{ \max \left[ V_t^{UP}(a_t, \varepsilon_t, v_t), V_t^{NOUP}(a_t, \varepsilon_t, v_t), 0 \right] \right\} \tag{5}$$

# Entry decision

- Every period there is free entry. New potential entrants, with endowment  $a_0$ , can learn their type  $v_0$  after having paid an initial cost  $S^C$ .
- Once they learn their type  $v_0$  (drawn from an initial uniform distribution), they decided whether or not to start activity.
- The free entry condition:

$$\int_{\underline{v}}^{\bar{v}} \max \{ E^{\varepsilon_0} [V_0(a_0, v_0, \varepsilon_0)], 0 \} f(v_0) dv_0 - S^C = 0 \quad (6)$$

# Calibration with risky innovation

Matched parameters				
	Value	Moment to match	Data	Model
$A$	5610	Aggregate sales		
$\delta$	0.03	employment share of exiting firms	8.2%	8%
$r$	1.02	average real interest rate	2%	2
$F$	0.2	average ratio fixed costs/labour costs	0.3	0.22
$\bar{v}$	1	normalized to 1.	n.a.	n.a.
$\underline{v}$	0.969	Cross sect. std. of firm average profits/added v.	0.084	0.036
$S^C$	0.6	mean profits/added value	0.036	0.031
$\xi$	0.3	avg. of time series vol of profits/added value	0.092	0.088
$\rho$	0.2	fraction of negative profits	0.21	0.21
$g$	1.0035	average yearly decline in profits/sales	3%	3%
$K$	0.02	average r&d/added value	3%	2%
$\xi^{NI}$	0.5	average age of firms	24	26.7
$\xi^I$	0.1	% of innovating firms (r&d to intr. new products)	13%	13%
$a_0$	0.4	% of firms going bankrupt every period	0.5%	0.5%

## Calibration with risky innovation (2)

## Other parameters

---

$\eta$	1.5	
$\sigma$	4	
$g^{fail}$	$g^3$	benchmark (sensitivity analysis)

# Simulate several industries

## With different degrees of financing frictions

Constrained :  $a_0 = 0.21$ , fraction of firms going bankrupt every period=1.5%

Benchmark:  $a_0 = 0.4$ , fraction of firms going bankrupt every period=0.5%

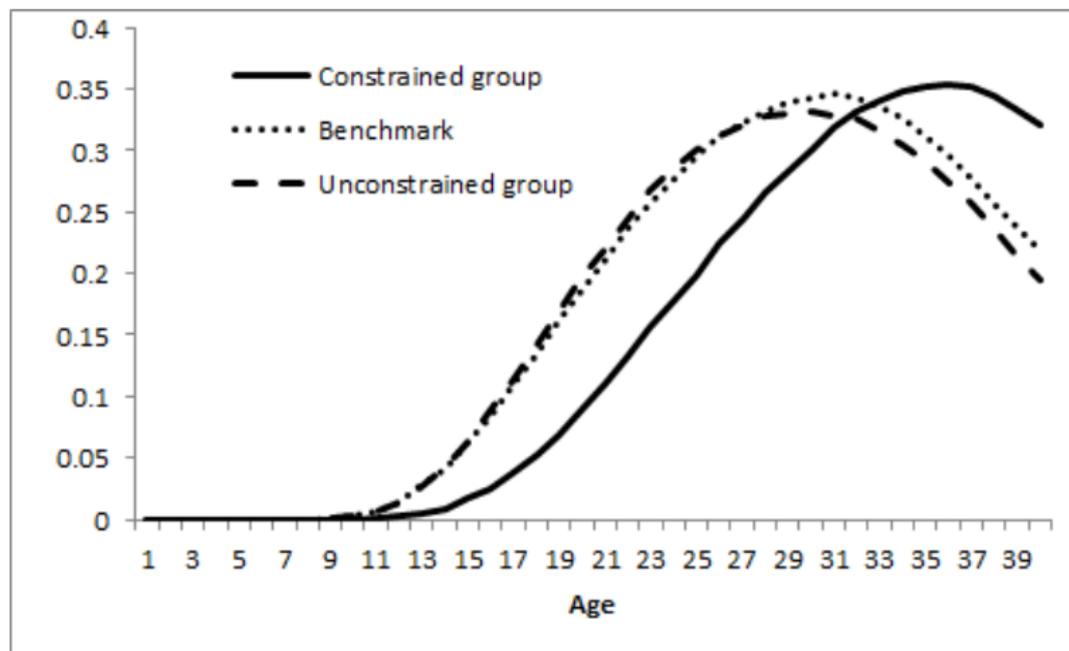
Unconstrained :  $a_0 = 2$ , fraction of firms going bankrupt every period=0.005%

## With different types of innovation

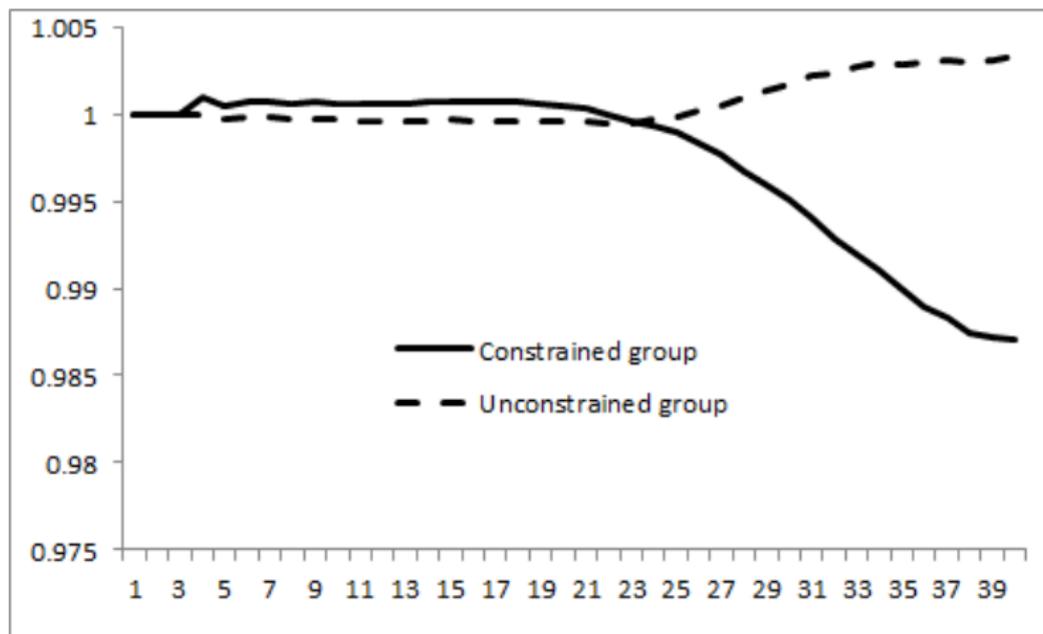
Embodied (risky) innovation:  $g^{fail} = 1.0105$

Disembodied (no downside risk) innovation:  $g^{fail} = 1$

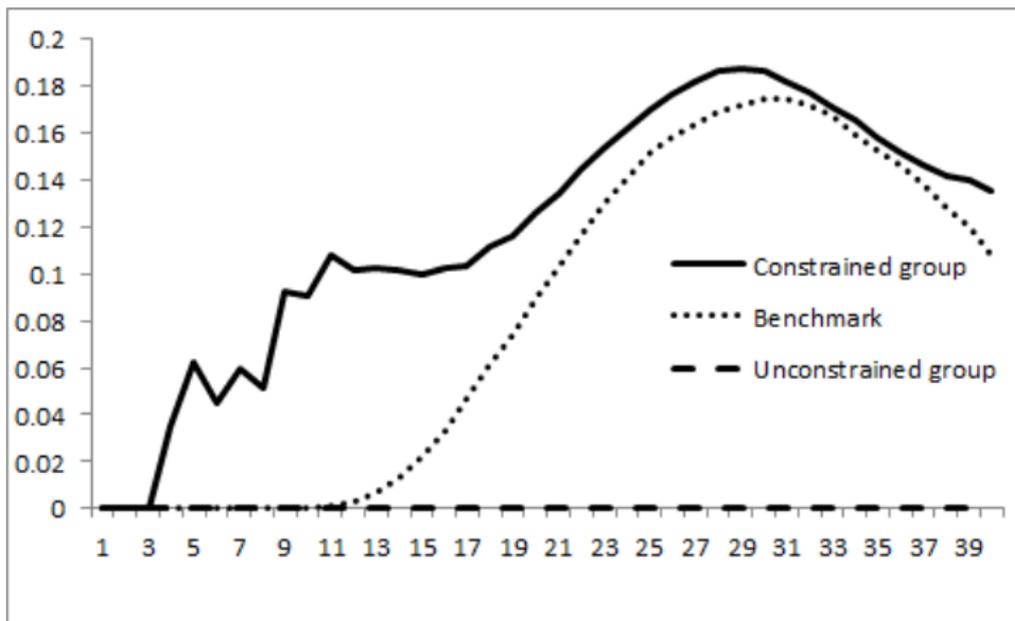
# Fraction of innovating firms in three industries conditional on age, RISKY INNOVATION



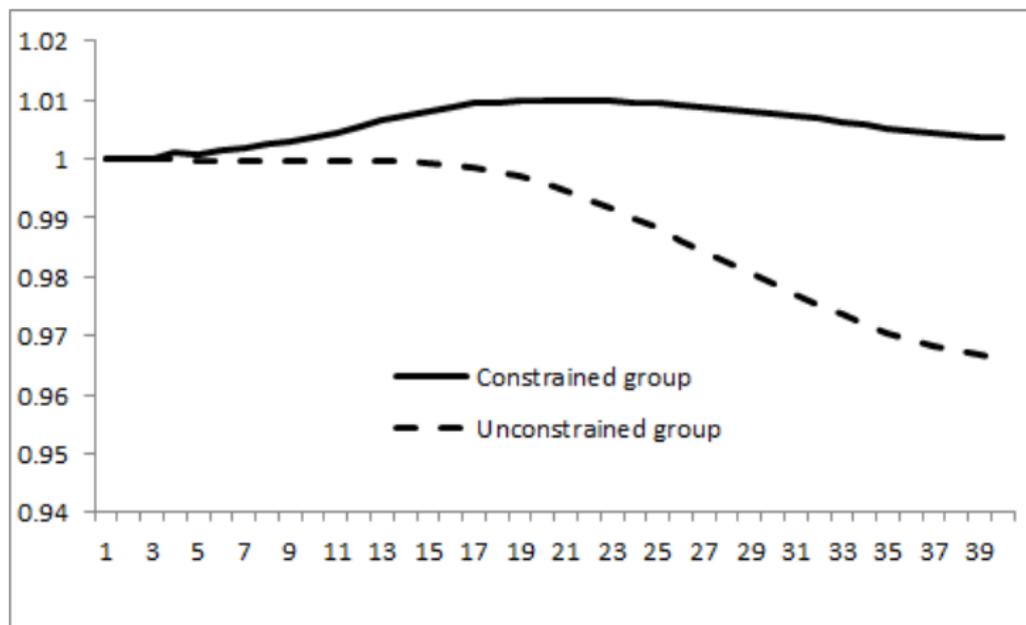
# Productivity conditional on age, relative to the benchmark case, RISKY INNOVATION



# Fraction of innovating firms in three industries conditional on age, "SAFE" INNOVATION

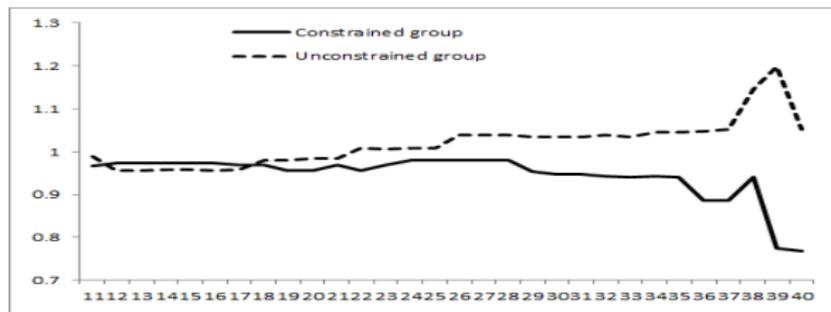


# Productivity conditional on age, relative to benchmark case, SAFE INNOVATION

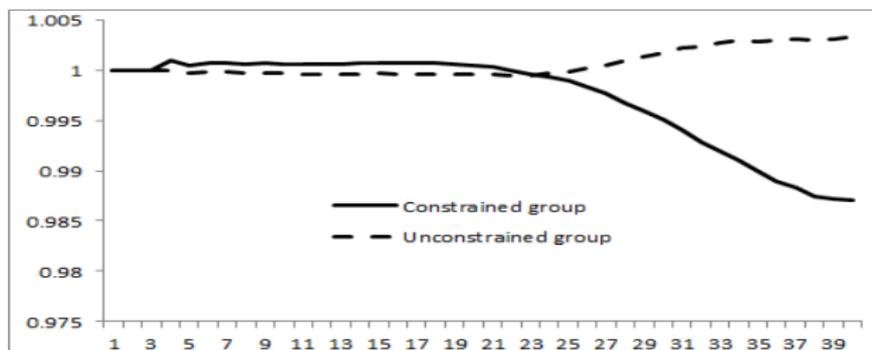


# Productivity conditional on age, comparison.

## Empirical data



## Risky Innovation



## Intuition of the result

- When there is no downside risk, current profits are compared with profits at the frontier.

## Intuition of the result

- When there is no downside risk, current profits are compared with profits at the frontier.
- More Financing frictions → fewer firms survive → less competition → profits increase for all productivity levels, but relatively more at the frontier. Firms start to innovate earlier in the lifecycle.

# Intuition of the result

- When there is no downside risk, current profits are compared with profits at the frontier.
- More Financing frictions→fewer firms survive→less competition→ profits increase for all productivity levels, but relatively more at the frontier. Firms start to innovate earlier in the lifecycle.
- When innovation is risky, the downside risk also matters.

# Intuition of the result

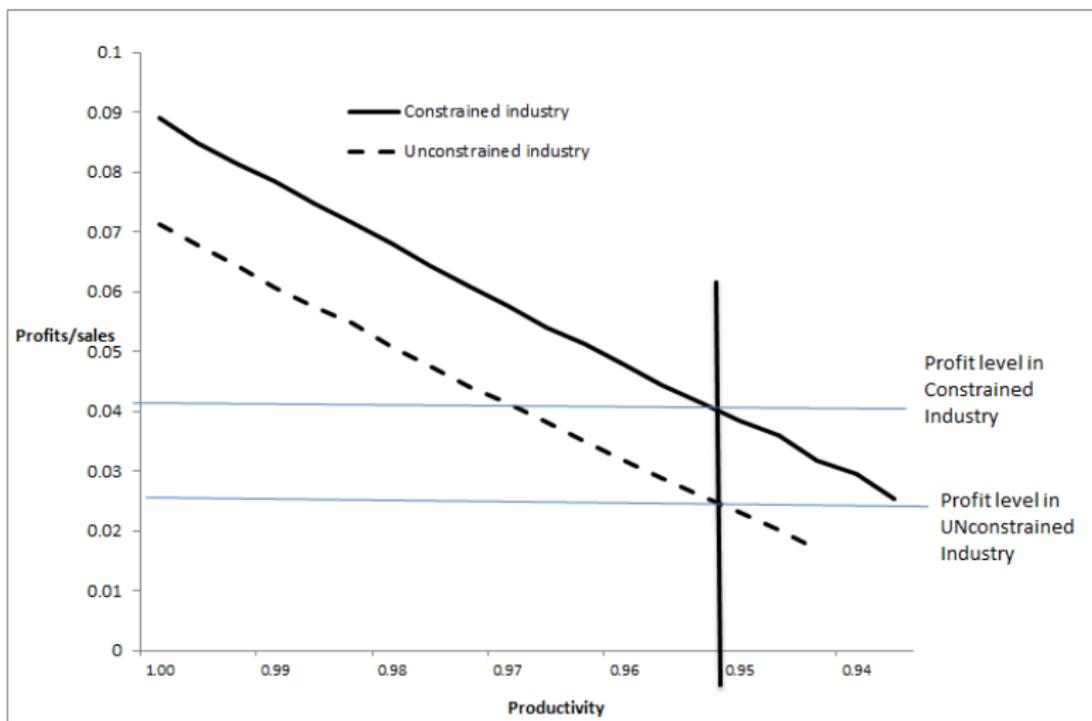
- When there is no downside risk, current profits are compared with profits at the frontier.
- More Financing frictions→fewer firms survive→less competition→ profits increase for all productivity levels, but relatively more at the frontier. Firms start to innovate earlier in the lifecycle.
- When innovation is risky, the downside risk also matters.
- Less Financing frictions→more firms survive→more competition→ profits decrease for all productivity levels. Firms have less to lose. (because if innovation fail, they can always exit and cut further losses), they start to innovate earlier.

# Conclusions

- In a calibrated model with heterogenous firms, potentially the most important effect of financing frictions on innovation is the indirect competition effect.
- Such effect is ambiguous and it depends on the nature of innovation.
- Preliminary empirical analysis is consistent with a negative effect of financing frictions on innovation because of downside innovation risk.

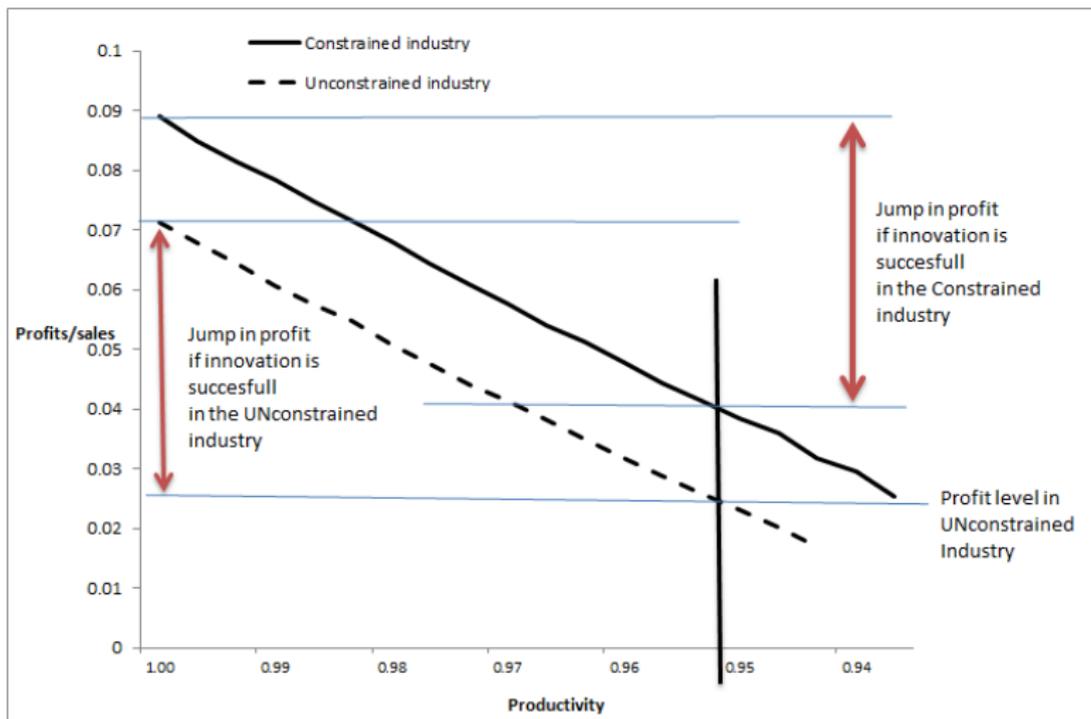
# Graphical intuition of the result - 1

First step: consider profit levels at a certain productivity level, in the two industries



## Graphical intuition of the result - 2

If there is no downside risk, the upside is what matters, and this is larger in the Constrained industry



# Graphical intuition of the result - 3

With downside risk, the potential maximum fall in profits also matters, and this is larger in the Constrained industry

